Cambridge
IGCSE

## Cambridge International Examinations

Cambridge International General Certificate of Secondary Education


## CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/51
Paper 5 (Core)
May/June 2015
1 hour
Candidates answer on the Question Paper.
Additional Materials: Graphics Calculator

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
Do not use staples, paper clips, glue or correction fluid.
You may use an HB pencil for any diagrams or graphs.
DO NOT WRITE IN ANY BARCODES.
Answer all the questions.
You must show all relevant working to gain full marks for correct methods, including sketches.
In this paper you will also be assessed on your ability to provide full reasons and communicate your mathematics clearly and precisely.
At the end of the examination, fasten all your work securely together.
The total number of marks for this paper is 24 .

Answer all the questions.

## INVESTIGATION

## STAIRCASES

This investigation looks at the number of cubes that make different types of staircase.
1 This is an UP staircase of height 3 made using 6 cubes.
It is a 3-step UP staircase because it has a height of 3 cubes.

(a) Write down the number of cubes that make an UP staircase of height 2.
(b) On the grid below draw an UP staircase of height 4.

(c) Complete the table for the number of cubes that make these UP staircases.

| Height | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number <br> of cubes | 1 |  | 6 |  |  |  |

(d) Find how many cubes make an UP staircase of height 10.
(e) (i) What is the height of the tallest UP staircase that can be made from 100 cubes?
(ii) Find how many cubes would be left over.

2 This is an UP AND DOWN staircase of height 3 made using 9 cubes.
It is a 3-step UP AND DOWN staircase because it has a height of 3 cubes.

(a) Find how many cubes make an $U P A N D ~ D O W N$ staircase of height 4.
(b) On the grid below draw an $U P A N D D O W N$ staircase of height 2 .

(c) Complete the table for the number of cubes that make these $U P A N D D O W N$ staircases.

| Height | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number <br> of cubes | 1 |  | 9 |  |  |  |

(d) The numbers of cubes form a sequence.

Write down the mathematical name of this sequence.
(e) Find how many cubes make an $U P$ AND $D O W N$ staircase of height 10 .
(f) Find an expression, in terms of $n$, for the number of cubes that make an UP AND DOWN staircase of height $n$.

3 This is a DOUBLE staircase of height 3 made using 12 cubes.
It is a 3-step $D O U B L E$ staircase because it has a height of 3 cubes.

(a) Find how many cubes make a $D O U B L E$ staircase of height 2.
(b) Complete the table for the number of cubes that make these DOUBLE staircases.

| Height | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number <br> of cubes | 2 |  | 12 |  |  |  |

(c) Find how many cubes make a DOUBLE staircase of height 10 .
(d) (i) Find an expression, in terms of $n$, for the number of cubes that make a DOUBLE staircase of height $n$.
(ii) Find the height of a DOUBLE staircase made from 240 cubes.
(e) Write down the connection between the number of cubes that make a DOUBLE staircase and the number of cubes that make an $U P A N D ~ D O W N$ staircase, when both staircases have the same height.
$\qquad$
$\qquad$

4 (a) Write down the connection between the number of cubes that make a DOUBLE staircase and the number of cubes that make an UP staircase, when both staircases have the same height.
$\qquad$
$\qquad$
(b) Find an expression, in terms of $n$, for the number of cubes that make an UP staircase of height $n$.

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